



▶▶ Under the patronage of **H.E. Dr. Abdullah Belhaif Al Nuaimi** - Minister of Infrastructure Development



▶▶ 17<sup>th</sup> Edition

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Under the Theme:

**Enhancing Maintenance  
Through Big Data Management**

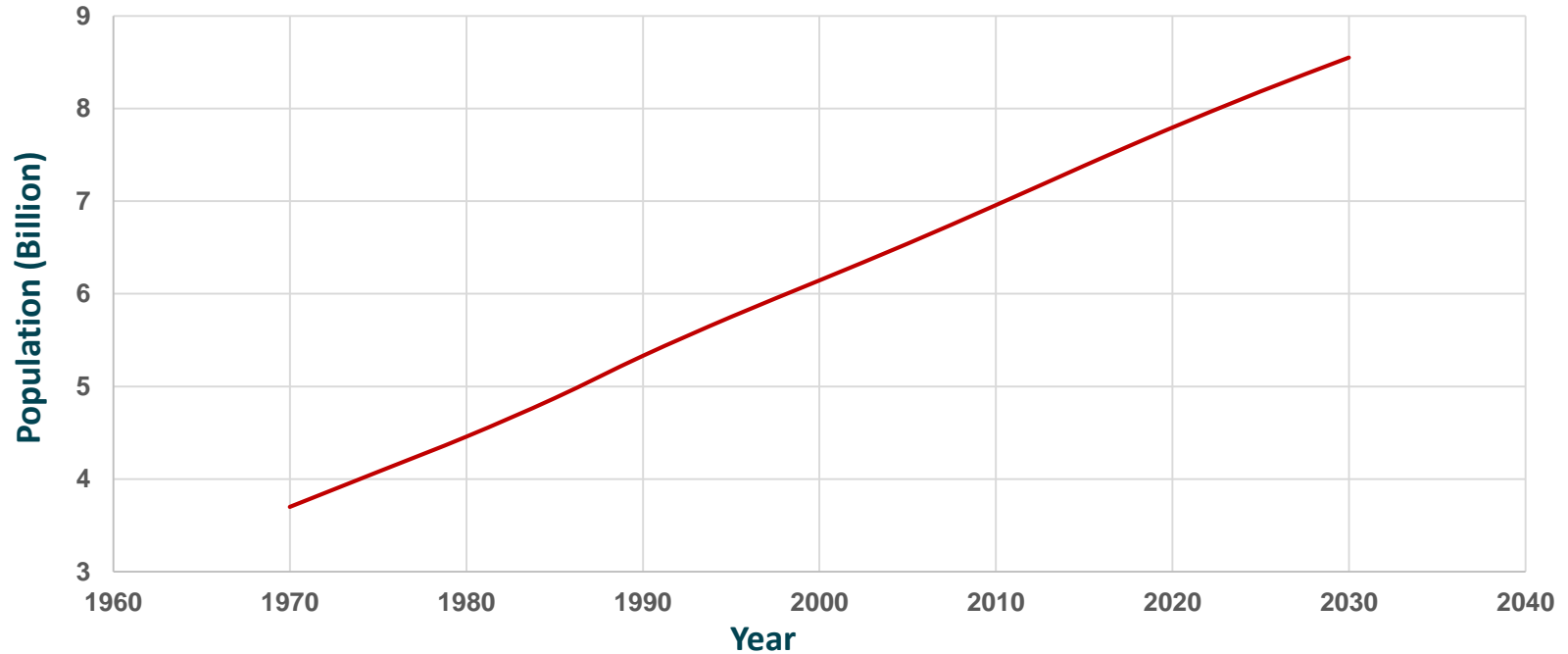
▶▶ **Environmental Economic  
Dispatch of  
Thermal Power Plants in  
Saudi Arabia: A Case Study**

# ▶▶ INTRODUCTION

- **The world demand for electricity is increasing in exponential manner with population**
- **There are more than 7.8 billion people now on the planet (Fig.1)**

# ▶▶ INTRODUCTION

## World Population



# ▶▶ INTRODUCTION



## Environment Issues

- CO<sub>2</sub> and NO<sub>x</sub> effects
- Health Issues
- Environmental Issues

## Vision 2030

- Decrease consumption of oil
- Renewable Energy

# ▶ ENVIRONMENTAL ECONOMIC DISPATCH: PROBLEM FORMULATION

The problem is to minimize the total fuel cost

$$\sum_{i=1}^n C_i = \sum_{i=1}^n a_i P_i^2 + b_i P_i + c_i$$

Where

|                      |                                     |
|----------------------|-------------------------------------|
| $C_i$                | Fuel cost of power plant i          |
| $a_i, b_i$ and $c_i$ | Cost coefficients of power plant i  |
| $n$                  | Number of controllable power plant. |
| $P_i$                | Power output of power plant i       |

# ▶ ENVIRONMENTAL ECONOMIC DISPATCH: PROBLEM FORMULATION

## Equality constraints

$$P_T = P_D + P_{loss}$$

Where

|            |                       |
|------------|-----------------------|
| $P_T$      | Total generated power |
| $P_{loss}$ | Transmission Loss     |
| $P_D$      | Total Load Demand     |

## Inequality constraints

$$P_{i,min} \leq P_i \leq P_{i,max}$$

# ▶ ENVIRONMENTAL ECONOMIC DISPATCH: PROBLEM FORMULATION

Transmission Loss can be found by

$$P_{loss} = \sum_{i=1}^n \sum_{j=1}^n P_i B_{ij} P_j$$

Where

$P_i$  Power output of power plant i

$P_j$  Power output of power plant j

$B_{ij}$  Losses Matrix

The input is the system load demand and the output is economic power generation and environmental emissions of various power plants

# ▶▶ ENVIRONMENTAL ECONOMIC DISPATCH: PROBLEM FORMULATION

For CO<sub>2</sub> Constraints

$$\sum_{i=1}^n E1_i = \sum_{i=1}^n d1_i P_i^2 + e1_i P_i + f1_i$$

Where

$E1_i$

$d1_i, e1_i$  and  $f1_i$

Total emission of CO<sub>2</sub> for power plant  $i$

CO<sub>2</sub> emission coefficients of power plant  $i$



# ▶▶ ENVIRONMENTAL ECONOMIC DISPATCH: PROBLEM FORMULATION

For  $\text{NO}_x$  constraints

$$\sum_{i=1}^n E_{2i} = \sum_{i=1}^n d_{2i}P_i^2 + e_{2i}P_i + f_{2i}$$

Where

$E_{2i}$

$d_{2i}, e_{2i}$  and  $f_{2i}$

Total emission of  $\text{NO}_x$  for power plant  $i$

$\text{NO}_x$  emission coefficients of power plant  $i$

# ▶▶ ENVIRONMENTAL ECONOMIC DISPATCH: PROBLEM FORMULATION

Total augmented cost can be obtained by

$$\sum_{i=1}^n Ct_i = \sum_{i=1}^n (w_1C_i + w_2E1_i + w_3E2_i)$$

# ▶▶ ENVIRONMENTAL ECONOMIC DISPATCH: PROBLEM FORMULATION

Different emission conditions may occur by varying  $w_1$ ,  $w_2$  and  $w_3$  as

| $w_1$ | $w_2$ | $w_3$ | Dispatch Type  |
|-------|-------|-------|--|
| 1     | 0     | 0     | Economic Dispatch (ED)   |
| 0     | 1     | 0     | Environmental Dispatch with CO <sub>2</sub> Emission Constraints (ED - CO <sub>2</sub> emission) |
| 0     | 0     | 1     | Environmental Dispatch with NO <sub>x</sub> Emission Constraints (ED - NO <sub>x</sub> emission) |
| 0.5   | 0.25  | 0.25  | Combined Environmental Economic Dispatch (EED)   |

# ▶ ENVIRONMENTAL ECONOMIC DISPATCH ALGORITHM

For The sequence of major computations of the algorithm is as follows:

i. Get the total load demand data

ii. Assume the load demand is distributed equally among all the thermal plants and there are no losses and set the Lagrange multiplier  $\frac{dC}{dP} = \lambda$

iii. Calculate the  $P_i$  of each power plant by using the coordination equation  $\frac{dC}{dP_i} + \lambda \frac{\partial P_{loss}}{\partial P_i} = \lambda$

# ▶▶ ENVIRONMENTAL ECONOMIC DISPATCH ALGORITHM

iv. Check the inequality by  $P_{i,min} \leq P_i \leq P_{i,max}$

v. Calculate the power loss by

vi. Check if  $\left| \sum P_i - (P_D + P_{loss}) \right| < \varepsilon$

Where  $\varepsilon$  is the assigned tolerance. If Yes, proceed to print the results; If No, modify the value of  $\lambda$  and go back to step – iii.

# ►► SYSTEM DATA

## System Data: Power plants and the Loss Coefficients

| Power Plant no. | a        | b       | c       | P min (MW) | P max (MW) |
|-----------------|----------|---------|---------|------------|------------|
| 1               | 0.001540 | 8.2716  | 225.360 | 1384       | 5538       |
| 2               | 0.000950 | 9.2233  | 253.050 | 381        | 1527       |
| 3               | 0.012490 | 11.8000 | 153.330 | 103        | 412        |
| 4               | 0.000885 | 8.8167  | 197.050 | 171        | 684        |
| 5               | 0.011040 | 7.7918  | 201.280 | 420        | 1680       |
| 6               | 0.050400 | 7.9664  | 217.110 | 206        | 827        |
| 7               | 0.016280 | 7.8225  | 213.440 | 123        | 494        |

# ►► SYSTEM DATA

## CO<sub>2</sub> Emissions Coefficients

| Power Plant no. | $d_1$  | $e_1$   | $f_1$    |
|-----------------|--------|---------|----------|
| 1               | 0.2651 | -61.02  | 5080.148 |
| 2               | 0.1401 | -29.952 | 3824.77  |
| 3               | 0.1059 | -9.5528 | 1342.851 |
| 4               | 0.1064 | -12.736 | 1819.625 |
| 5               | 0.1059 | -9.5528 | 1342.851 |
| 6               | 0.4031 | -121.98 | 11381.07 |
| 7               | 0.1064 | -12.736 | 1819.625 |

# ►► SYSTEM DATA

## NO<sub>x</sub> Emissions Coefficients

| Power Plant | $d_2$    | $e_2$    | $f_2$  |
|-------------|----------|----------|--------|
| 1           | 0.006323 | -0.38128 | 80.90  |
| 2           | 0.006480 | -0.79027 | 28.82  |
| 3           | 0.003174 | -1.36061 | 324.20 |
| 4           | 0.006732 | -2.39928 | 610.30 |
| 5           | 0.003174 | -1.36061 | 324.20 |
| 6           | 0.006181 | -0.39077 | 50.81  |
| 7           | 0.006732 | -2.39928 | 610.30 |



# ►► SYSTEM DATA

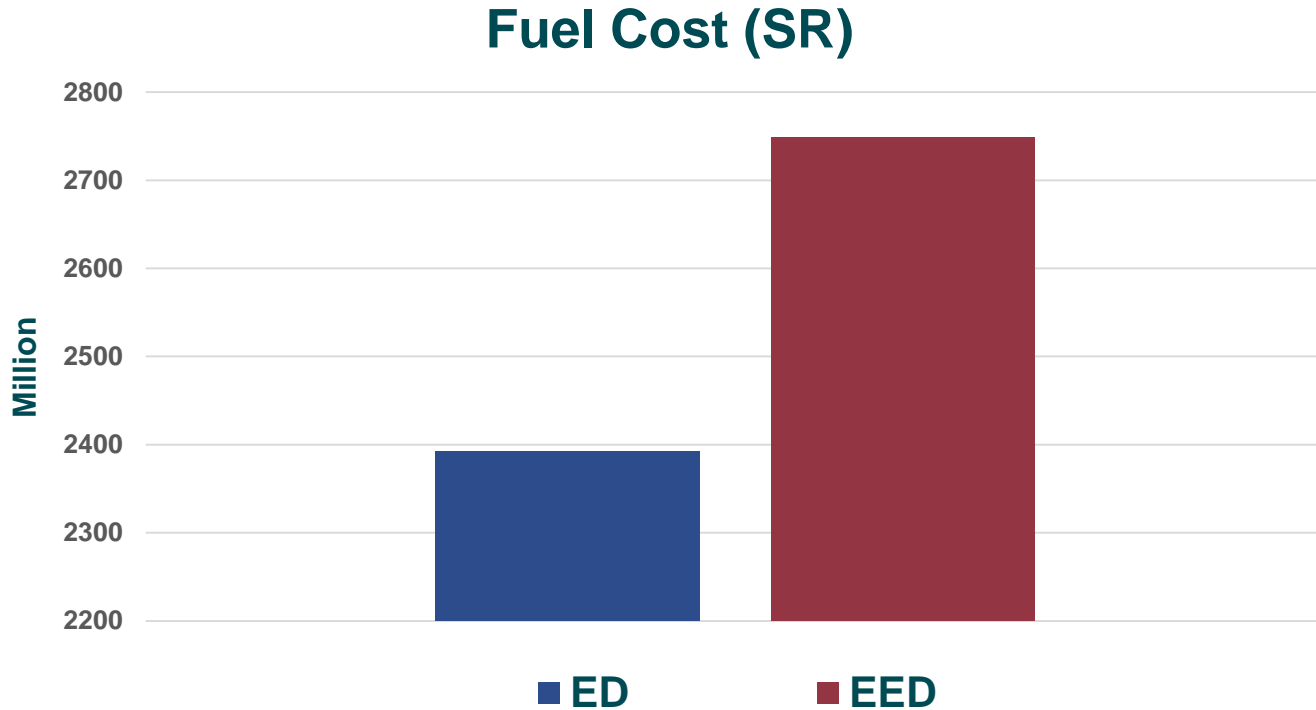
## The Losses matrix B

$$B = 10^{-5} * \begin{bmatrix} 2.0 & 1.0 & 0.15 & 0.005 & 0.001 & -0.03 & 0.02 \\ 1.0 & 3.0 & -0.02 & 0.01 & 0.012 & 0.01 & -0.1 \\ 0.15 & -0.02 & 0.1 & -0.1 & 0.1 & 0.001 & 0.04 \\ 0.005 & 0.01 & -0.1 & 15.0 & 0.06 & 5.0 & 0.15 \\ 0.001 & 0.012 & 0.1 & 0.06 & 0.4 & 2.0 & 0.01 \\ -0.03 & 0.01 & 0.001 & 5.0 & 2.0 & 0.5 & 0.4 \\ 0.02 & -0.1 & 0.04 & 0.15 & 0.01 & 0.4 & 0.1 \end{bmatrix}$$

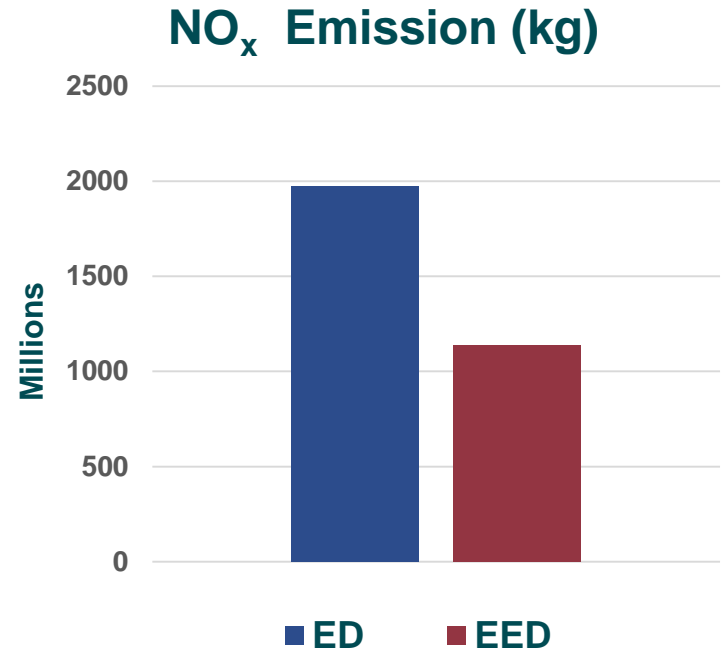
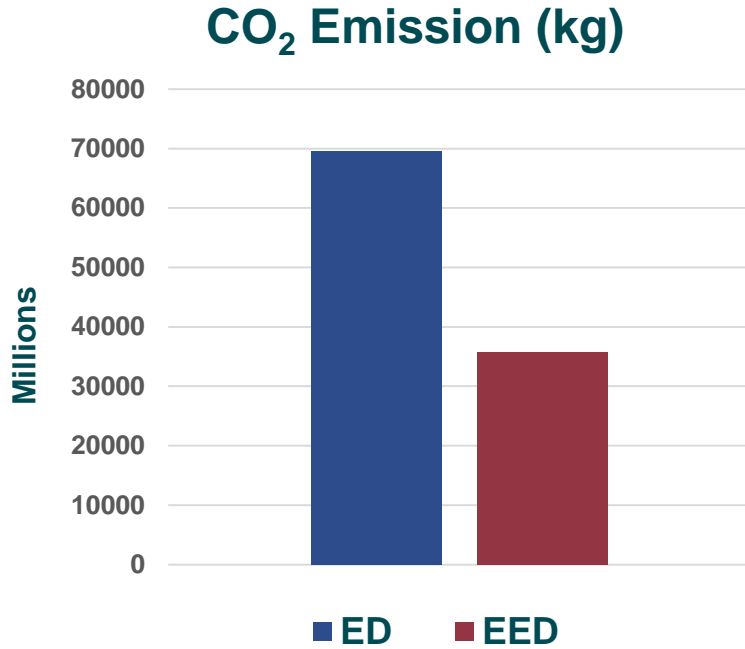
# ▶▶ ANNUAL COST AND EMISSION RESULTS

|                                 | Economic Dispatch |            |             |                                   | Environmental Economic Dispatch |          |             |                                   | % Difference in Annual Estimates |
|---------------------------------|-------------------|------------|-------------|-----------------------------------|---------------------------------|----------|-------------|-----------------------------------|----------------------------------|
|                                 | Typical Day       |            |             | Total Annual Estimate in millions | Typical Day                     |          |             | Total Annual Estimate in millions | [(A-B)/A] *100                   |
|                                 | Winter            | Summer     | During Hajj | (A)                               | Winter                          | Summer   | During Hajj | (B)                               |                                  |
| Fuel Cost (SR/h)                | 152686.6          | 339077.3   | 337047.1    | 2392.8                            | 153137.3                        | 400678   | 398166      | 2748.9                            | 14.88                            |
| CO <sub>2</sub> Emission (kg/h) | 2088059.8         | 11036398.0 | 10972840.9  | 69583.2                           | 202044                          | 5206331  | 5299453.9   | 35807.3                           | 48.54                            |
| NO <sub>x</sub> Emission (kg/h) | 68151.3           | 308328.9   | 306746.9    | 1972.2                            | 64426.0                         | 165229.2 | 167374.61   | 1137.2                            | 42.34                            |

# ▶▶ SIMULATION RESULTS



# ▶▶ SIMULATION RESULTS



## ►► CONCLUSION

- This paper has discussed a case study of the application of environmental economic dispatch on the Saudi Western Operating Grid having seven thermal power plants.
- The environments constraints on CO<sub>2</sub> and NO<sub>x</sub> have been considered
- It can be seen that EED leads significant reduction in the environmental pollution without any major increase in the cost



**Thank You**